

Homework 3

1) Generate 1000 X from $\text{GAM}(3,2)$ distribution (This is an abbreviation for gamma distribution with $\alpha = 3$ and $\beta = 2$. See page 624 in Casella and Berger as well as `rgamma`, `pgamma`, `dgamma`, and `qgamma` function in R). Compare empirical density and cdf with true density and cdf. Generate $Y \sim \text{UNIF}(0,1)$ using probability integral transformation and verify that empirical cdf is similar to true cdf. Next, generate 1000 U from $\text{UNIF}(0,1)$ and then generate $V \sim \text{GAM}(3,2)$ using the inverse cdf of a gamma distribution. Compare empirical density and cdf with true density and cdf. Please turn in plots of your simulations as well as printout of your code.

2) Let X be a non-negative continuous random variable with CDF $F(x)$ and $E(X) < \infty$. Show that $E(X) = \int_0^{\infty} (1 - F(x)) dx$.

Casella and Berger Book: 2.1, 2.2, 2.3, 2.4, 2.6 (don't need to show pdf integrates to 1), 2.8 (don't need to show it's a cdf), 2.15, 2.20, 2.24, 2.33